

EXAM - 22 May 2014  
ELT-47246 Passive RF Circuits

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**Examiner:** Toni Björninen

**Calculator:** Allowed (also programmable).

**Additional instructions:** Use also written explanations – normally a computation alone does not convey all the relevant information. A collection of formulas is provided.

**Problem 1. Concept test.**

Select the all the correct statements – no further justifications needed. Correct choice: plus 1 point. Incorrect choice: minus 1 point (negative total score will be set to zero).

**Q1:** Basic concepts.

- (a) At a high frequency, a shunt capacitor may be replaced with an open-ended transmission line stub
- (b) There is no equivalent transmission line stub configuration to represent an inductor at high frequencies
- (c) Quarter-wave transformer is used to transform a resistive load to a desired resistance
- (d) A finite and non-zero complex impedance can always be matched to a given non-zero resistance using two purely reactive lumped components

**Q2:** Your task is to design a microstrip transmission line with the characteristic impedance of  $50 \Omega$  on a typical dielectric circuit board. To complete the task with engineering precision you need to know...

- (a) Relative permittivity of the board material
- (b) Loss tangent of the board material
- (c) Thickness of the board
- (d) Conductivity of the board metallization

**Q3:** Your task is to impedance-match an antenna to a  $50 \Omega$  source. With your current matching circuit, the input reflection coefficient is  $-17 \text{ dB}$ , but this is still  $3 \text{ dB}$  from the design goal:  $-20 \text{ dB}$ .

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- (a) The matching is not good enough to safely feed the antenna: the signal reflected back to the source is likely to damage it.
- (b) Due to imperfect matching, the power delivered to the antenna from the source is only 50% of the target.
- (c) Here the  $3 \text{ dB}$  difference has little impact on the power transfer from the source to antenna.

**Problem 2. Transmission lines.**

Consider a loss-free  $50 \Omega$  transmission line with the length of  $d = \lambda/8$ . Suppose the line is terminated with load impedance of  $150 \Omega$ . Determine the

- (a) Input impedance
- (b) Input reflection coefficient in a  $50 \Omega$  system
- (c) Voltage amplitude at the center point of the line when it is fed from a  $5 \text{ V}$  source with the internal impedance of  $50 \Omega$

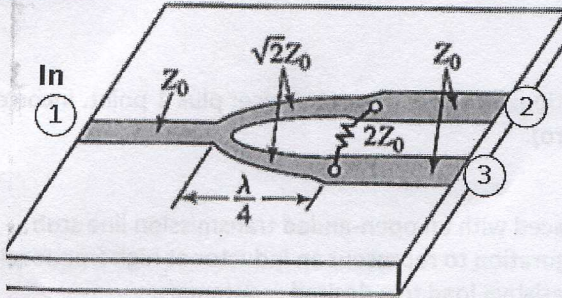
**Problem 3. Passive microwave components.**

Name the below components and briefly explain their operation when an excitation is applied at port(s) labelled with "in". Determine which of the properties: loss-free, reciprocal and matched are associated with each component.



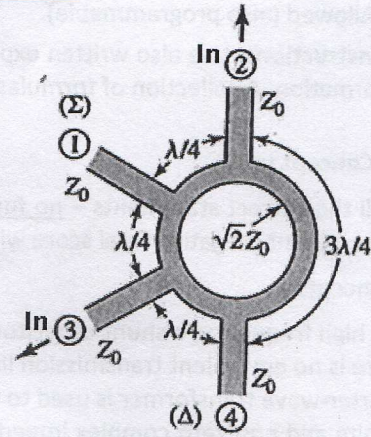
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Component 1

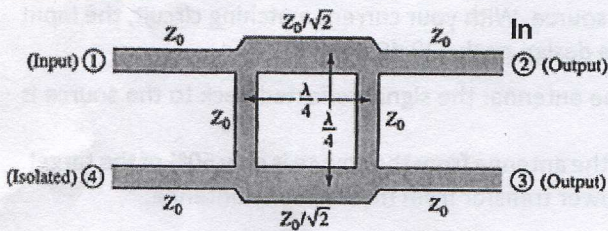


$$S = \frac{-j}{\sqrt{2}} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

Component 3



Component 2



$$S = \frac{-1}{\sqrt{2}} \begin{pmatrix} 11 & 12 & 13 \\ 0 & j & 1 & 0 \\ j & 0 & 0 & -1 \\ 1 & 0 & 0 & j \\ 0 & -1 & j & 0 \end{pmatrix}$$



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$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} \quad \lambda = \frac{c_0}{f\sqrt{\epsilon_r\mu_r}} \quad \gamma = \alpha + j\beta \quad \beta = \frac{2\pi}{\lambda}$$

$$V(z) = V_f e^{-\gamma z} + V_b e^{\gamma z}$$

$$I(z) = I_f e^{-\gamma z} + I_b e^{\gamma z}$$

$$Z_{in} = Z_0 \frac{Z_L + jZ_0 \tan(\beta l)}{Z_0 + jZ_L \tan(\beta l)}$$

$$\frac{V_f}{I_f} = Z_0 = -\frac{V_b}{I_b}$$

$$\Gamma_L = \frac{V_b(0)}{V_f(0)} = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$\Gamma_{in} = \frac{V_b(-d)}{V_f(-d)} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = \Gamma_L e^{-2\gamma d}$$

$$\mathbf{S}^* \mathbf{S} = \mathbf{U}$$