

Problem 3 (max 5 points)

Transfer function matrix of a grid-connected photovoltaic inverter is given at open-loop in (1).

- Draw the control block diagrams that represent the inverter output dynamics in dq-domain and include the output current controllers, sensing gains and PWM modulator gain.
- Draw a control block diagram where cascaded control scheme is implemented to regulate the PV voltage. You can assume that DC-side dynamics depend mainly on d-components and that cross-couplings between d and q-components can be neglected.
- Use the control block diagram to solve the transfer function of the DC voltage control loop gain.
- Explain the tuning process of the cascaded control loops.
- Solve the output admittance q-component from the block diagram. You can assume the output current q-component is not affected by any of the d-components.

$$\begin{bmatrix} \hat{v}_{PV} \\ \hat{i}_{od} \\ \hat{i}_{oq} \end{bmatrix} = \begin{bmatrix} G_{11}^{OL} & G_{12}^{OL} & G_{13}^{OL} & G_{14}^{OL} & G_{15}^{OL} \\ G_{21}^{OL} & G_{22}^{OL} & G_{23}^{OL} & G_{24}^{OL} & G_{25}^{OL} \\ G_{31}^{OL} & G_{32}^{OL} & G_{33}^{OL} & G_{34}^{OL} & G_{35}^{OL} \end{bmatrix} \begin{bmatrix} \hat{i}_{pV} \\ \hat{v}_{od} \\ \hat{v}_{oq} \\ \hat{d}_d \\ \hat{d}_q \end{bmatrix} \quad (1)$$

Problem 4 (max 5 points)

Three-phase LCL-filter is shown in Figure 3. Solve the average state-space model of the filter in the dq-domain. You can assume that the three-phase input and output voltages are balanced. The zero component can be neglected. Draw the electrical circuits of the filter in dq-domain (separately for d and q-components), $(\mathbf{x}^{\alpha\beta} = \mathbf{x}^{dq} \cdot e^{j\omega t})$, $(\mathbf{T}^{abc \rightarrow \alpha\beta} \cdot [k \ k \ k]^T = [0 \ 0 \ k]^T)$.

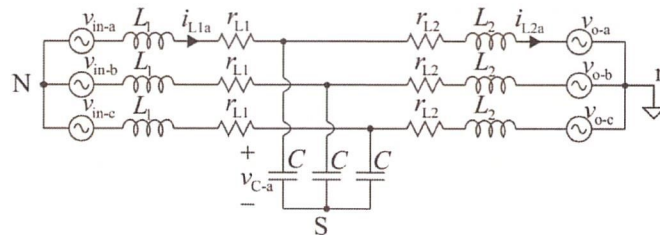


Figure 3: Three-phase LCL-type filter.

Hints:

$$\frac{d}{dt} i_{L1}^{dq} = f(v_{NS}, v_{in-d}, v_{in-q}, v_{C-d}, v_{C-q})?$$

$$\frac{d}{dt} v_C^{dq} = f(i_{L1d}, i_{L1q}, i_{L2d}, i_{L2q})?$$

$$\frac{d}{dt} i_{L2}^{dq} = f(v_{NS}, v_{C-d}, v_{C-q}, v_{o-d}, v_{o-q})?$$